

Difracção

$$U(x_0, y_0) = \frac{1}{i\lambda} \iint_{\Sigma} U(x_1, y_1) \frac{e^{ikr_{01}}}{r_{01}} \cos\theta dx_1 dy_1$$

$$U(x, y) = \frac{e^{ikz}}{i\lambda z} \iint_{-\infty}^{\infty} U(\xi, \eta) e^{-i\frac{k}{2z}[(x-\xi)^2 + (y-\eta)^2]} d\xi d\eta$$

$$U(x, y) = \frac{e^{ikz} e^{-i\frac{k}{2z}(x^2+y^2)}}{i\lambda z} \iint_{-\infty}^{\infty} U(\xi, \eta) e^{-i\frac{2\pi}{\lambda z}(x\xi+y\eta)} d\xi d\eta = \frac{e^{ikz} e^{-i\frac{k}{2z}(x^2+y^2)}}{i\lambda z} \mathcal{F}\{U\}_{f_X=\frac{x}{\lambda z}, f_Y=\frac{y}{\lambda z}}$$

Transformação de Fourier

$$\mathcal{F}\{g\} = G(f_X, f_Y) = \iint_{-\infty}^{\infty} g(x, y) e^{-i2\pi(f_X x + f_Y y)} dx dy$$

$$\iint_{-\infty}^{\infty} |g(x, y)|^2 dx dy = \iint_{-\infty}^{\infty} |G(f_X, f_Y)|^2 df_X df_Y$$

$$\mathcal{F}^{-1}\{G\} = g(x, y) = \iint_{-\infty}^{\infty} G(f_X, f_Y) e^{+i2\pi(f_X x + f_Y y)} df_X df_Y$$

$$g \star\star \delta = \iint_{-\infty}^{\infty} g(x, y) \delta(x - \xi, y - \eta) dx dy = g(\xi, \eta)$$

$$\mathcal{F} \left\{ \iint_{-\infty}^{\infty} g(\xi, \eta) h(x - \xi, y - \eta) d\xi d\eta \right\} = G(f_X, f_Y) H(f_X, f_Y)$$

$$\mathcal{F}\{g(x, y)\} = \mathcal{F}^{-1}\mathcal{F}\{g(x, y)\} = g(x, y)$$

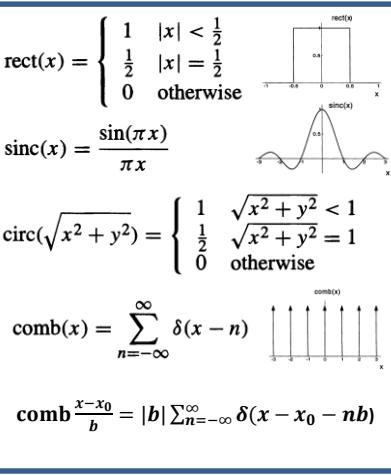
$$\mathcal{F}\{gh\} = G(f_X, f_Y) \star\star H(f_X, f_Y)$$

$$\mathcal{F}\{g(x-a, y-b)\} = G(f_X, f_Y) e^{-i2\pi(f_X a + f_Y b)}$$

$$\mathcal{F}\{\iint_{-\infty}^{\infty} g(\xi, \eta) g^*(\xi - x, \eta - y) d\xi d\eta\} = \mathcal{F}\{g \otimes \overline{g}\} = |G(f_X, f_Y)|^2$$

$$\mathcal{F}\{g(ax, by)\} = \frac{1}{|ab|} G\left(\frac{f_X}{a}, \frac{f_Y}{b}\right)$$

J. Goodman, Introduction to Fourier Optics (3ª edição, 2005), Cap. 2



Function	Transform
$\exp[-\pi(a^2 x^2 + b^2 y^2)]$	$\frac{1}{ ab } \exp\left[-\pi\left(\frac{f_X^2}{a^2} + \frac{f_Y^2}{b^2}\right)\right]$
$\text{rect}(ax) \text{rect}(by)$	$\frac{1}{ ab } \text{sinc}(f_X/a) \text{sinc}(f_Y/b)$
$\delta(ax, by)$	$\frac{1}{ ab }$
$\exp[j\pi(ax + by)]$	$\delta(f_X - a/2, f_Y - b/2)$
$\text{comb}(ax) \text{comb}(by)$	$\frac{1}{ ab } \text{comb}(f_X/a) \text{comb}(f_Y/b)$
$\exp[j\pi(a^2 x^2 + b^2 y^2)]$	$\frac{j}{ ab } \exp\left[-j\pi\left(\frac{f_X^2}{a^2} + \frac{f_Y^2}{b^2}\right)\right]$
$\exp[-(a x + b y)]$	$\frac{1}{ ab } \frac{2}{1 + (2\pi f_X/a)^2} \frac{2}{1 + (2\pi f_Y/b)^2}$

$$\cos(2\pi f_0 x) = \frac{e^{+i2\pi f_0 x} + e^{-i2\pi f_0 x}}{2}$$

$$\frac{1}{2} [\delta(f_X - f_0) + \delta(f_X + f_0)]$$

$$\sin(2\pi f_0 x) = \frac{e^{+i2\pi f_0 x} - e^{-i2\pi f_0 x}}{2i}$$

$$\frac{1}{2i} [\delta(f_X - f_0) - \delta(f_X + f_0)]$$

Ondas

$$u(x, t) = \frac{f(x - ct) + f(x + ct)}{2} + \frac{1}{2c} \int_{x-ct}^{x+ct} g(s) ds$$

$$E(x) = \exp(-\alpha x) E(x=0) \quad [\text{W/m}^2]$$

$$f_o = f_s \left(\frac{v \pm v_o}{v \mp v_s} \right)$$

$$v_g = \frac{d\omega}{dk} \Big|_{(k_0, \omega_0)} \quad \mathcal{P} \sim \langle \left(\frac{d\psi}{du} \right)^2 \rangle$$

$$\psi(x, t) = a \cos(ku + \varphi)$$

$$\psi(x, t) = X(x) T(t)$$